

#1 (a.) $V_{peak} = A_0$ and $V_{rms} = \frac{V_{peak}}{\sqrt{2}}$

$$\therefore \boxed{V_{rms} = \frac{A_0}{\sqrt{2}}}$$

(b.) $I_{max} = \frac{\Delta V_{peak}}{X_c}$ where $X_c = \frac{1}{\omega C}$

$$\Rightarrow I_{max} = \omega C A_0$$

$$\therefore \boxed{C = \frac{I_{max}}{\omega A_0}}$$

#2 $\Delta V_{p-p} = 2\Delta V_{peak}$

$$I_{max} = \frac{\Delta V_{peak}}{Z} = \Delta V_{peak} \left[R^2 + (X_c - X_L)^2 \right]^{-1/2} \quad \text{and } \omega = 2\pi f$$

with $X_c = \frac{1}{2\pi f C}$ and $X_L = 2\pi f L$

$$(a.) \boxed{\Delta V_{max}^{AB} = \frac{1}{2} \Delta V_{p-p} R \left[R^2 + \left(\frac{1}{2\pi f C} - 2\pi f L \right)^2 \right]^{-1/2}}$$

$$(b.) \boxed{\Delta V_{max}^{BC} = \pi \Delta V_{p-p} f L \left[R^2 + \left(\frac{1}{2\pi f C} - 2\pi f L \right)^2 \right]^{-1/2}}$$

$$(c.) \boxed{\Delta V_{max}^{CD} = \frac{1}{4\pi} \frac{\Delta V_{p-p}}{f C} \left[R^2 + \left(\frac{1}{2\pi f C} - 2\pi f L \right)^2 \right]^{-1/2}}$$

(d.) $X_{tot}^{BD} = |X_c - X_L|$

$$\therefore \boxed{\Delta V_{max}^{BD} = \Delta V_{p-p} \frac{\left| \frac{1}{4\pi f C} - \pi f L \right|}{\sqrt{R^2 + \left(\frac{1}{2\pi f C} - 2\pi f L \right)^2}}}$$

$$\#3 \quad (a.) \quad X_L = \omega L$$

$$\therefore \boxed{X_L = 2\pi fL}$$

$$(b.) \quad I_{rms} = \frac{\Delta V_{rms}}{X_L}$$

$$\therefore \boxed{I_{rms} = \frac{\Delta V_{rms}}{2\pi fL}}$$

$$\#4 \quad \text{for } X_C = X_L \text{ we have } \frac{1}{\omega C} = \omega L$$

$$\Rightarrow \omega = \frac{1}{\sqrt{LC}} \text{ where } \omega = 2\pi f$$

\therefore for both parts (a.) and (b.)

$$\boxed{f = \frac{1}{2\pi\sqrt{LC}}}$$

$$\#5 \quad \omega_0 = 2\pi f_0$$

$$X_C = X_L$$

$$\Rightarrow LC = \frac{1}{\omega_0^2}$$

$$\Rightarrow C = \frac{1}{L\omega_0^2}$$

$$\therefore \boxed{C = \frac{1}{4\pi^2 f_0^2 L}}$$

$$\#6 \quad (a.) \quad X_L = 2\pi fL$$

$$(b.) \quad X_C = \frac{1}{2\pi fC}$$

$$(c.) \quad V_{\max} = Z I_{\max}$$

$$\therefore Z = \frac{V_{\max}}{I_{\max}}$$

$$(d.) \quad \phi = \tan^{-1} \left(\frac{X_L - X_C}{R} \right)$$

$$\therefore \phi = \tan^{-1} \left(\frac{2\pi fL - \frac{1}{2\pi fC}}{R} \right)$$

$$\#7 \quad R_{eq} = \left(\frac{N_1}{N_2} \right)^2 R_L$$

$$V_1 = \frac{N_1}{N_2} V_L \Rightarrow I_1 = \frac{V_1}{R_{eq}} = \frac{\frac{N_1}{N_2} V_L}{\left(\frac{N_1}{N_2} \right)^2 R_L} = \frac{N_2}{N_1} \frac{V_L}{R_L}$$

$$\Rightarrow \Delta V_{\text{drop}} = V_s - V_1 = V_s - \frac{N_1}{N_2} V_L$$

$$\therefore R_s = \frac{\Delta V_{\text{drop}}}{I_1} = \frac{V_s N_1 R_L}{N_2 V_L} - R_L$$

$$\therefore R_s = R_L \left(\frac{N_1}{N_2} \frac{V_s}{V_L} - 1 \right)$$

#8

$$(a.) V_{rms} = Z I_{rms}$$

$$\therefore \boxed{Z = \frac{V_{rms}}{I_{rms}}}$$

$$(b.) \frac{X_L - X_C}{R} = \tan \phi \text{ and } R^2 = Z^2 - (X_L - X_C)^2$$

$$\Rightarrow \frac{(X_L - X_C)^2}{Z^2 - (X_L - X_C)^2} = \tan^2 \phi$$

$$\Rightarrow (X_L - X_C)^2 = Z^2 \tan^2 \phi - (X_L - X_C)^2 \tan^2 \phi$$

$$\Rightarrow (X_L - X_C)^2 (1 + \tan^2 \phi) = Z^2 \tan^2 \phi \text{ where } 1 + \tan^2 \phi = \sec^2 \phi$$

$$\Rightarrow (X_L - X_C)^2 = Z^2 \frac{\tan^2 \phi}{\sec^2 \phi} = Z^2 \frac{\sin^2 \phi}{\cos^2 \phi} \cos^2 \phi$$

$$\therefore (X_L - X_C)^2 = Z^2 \sin^2 \phi$$

$$\therefore X_L - X_C = Z \sin \phi$$

$$\therefore \boxed{X_L - X_C = \frac{V_{rms}}{I_{rms}} \sin \phi}$$